Mini-task: Using a problem-solving approach

Using a problem-solving approach
When you are working out a numerical problem, it might help to use a problem-solving approach.
You can think of the problem in several stages:

- Making sense of the problem/situation
- Choosing the right calculation
- Making sense of the answer
- Checking your answer

This learner activity makes some suggestions to help you in each of these stages.

1. Making sense of the problem - What does it mean?

You can use your experience of the world to help you think about the problem in practical, everyday terms. It might help to visualise the problem.

## Sometimes it may help to sketch a diagram of the situation.

## Example 1: Drawing a sketch to help

A wardrobe is shown on a room plan as 2 cm long.
The scale of the plan is $1: 100$.
How long is the wardrobe in real life?

| For this example, drawing a sketch might help |  |  |  |
| :--- | :--- | :--- | :--- |
| Each cm on the plan will be 100 cm in real life |  |  |  |

If you would like more practice with this:
Look at the example situations in 'Mini-task: Which operation?' and think about which of the examples might be made easier by drawing a sketch.

## 2. Choosing the right calculation:

There are several things you need to think about:

- Pick out the key information needed to work out the right calculation.

Sometimes you may need to ignore some information - or numbers that are not important.

- Then decide whether to add $(+)$, subtract $(-)$, multiply $(\times)$ or divide $(\div)$.


## Example 2.1

Winston works different hours each week and is paid for the hours he has worked at $£ 5.25$ an hour. This week he worked 32 hours and earned $£ 168$.
He has to pay $£ 22$ in tax and National Insurance.
How much does he get in his pay packet?

To work out how much Winston gets, only some of the numbers given are relevant:
He earns $£ 168$ that week.
He pays $£ 22$ in tax and National Insurance. This is taken off his gross wage.
So the pay in his pay packet will be $£ 168-£ 22=£ 146$

Some questions might involve a calculation with more than one step:

## Example 2.2

Maya has a budget of $£ 100$ for a meal for 5 people. She spends $£ 13, £ 25$ and $£ 46$.
How much of her original budget has she got left?
To work out how much Maya has left, you might work this out in two steps:
Firstly, work out how much she has spent already:

$$
£ 13+£ 25+£ 46=£ 84
$$

Then you take this from the amount she had to start with:

$$
£ 100-£ 84=£ 16
$$

So she has:
£16 left

If you would like practice with choosing the right calculation, 'Mini-task: Which operation?' looks at:

- Changing questions in words into calculations
- Thinking about key words and phrases that give you clues about what you need to work out
- Picking out the information you need to answer the problem (and knowing what other information to ignore).


## 3. Making sense of the answer - units

When you get an answer, you need to make sense of it. You can often use your experience of the real world and think 'what does this answer mean?'.

## What units does the answer tell you about?

## Example 3

I am saving for a night out. I put aside $£ 9$ each week. How long will it take me to save up $£ 90$ for my friend's hen night?

| I decide that the calculation I need to work out is: $90 \div 9=10$ |
| :--- | :--- |
| But what does this answer mean?  <br> What units is the answer in? (10 whats?) <br> In this example, it will be: 10 weeks |

## For each of these questions, decide which units the answer will be in:

Q3(a) Three friends win $£ 18$ between them.
If they share it equally, how much will they each get?
Q3(b) Keith has a $£ 10$ note in his pocket. How many drinks at $£ 1.99$ can he afford?
Q3(c) Someone working in an office is leaving. The other 5 people in the office decide that they want to buy her a leaving present.
The present they have in mind costs $£ 30$. How much do each of the office mates need to contribute?

Q3(d) Mac wants to put aside some money every month to pay for his car road tax. He needs to save up $£ 96$ over the year ( 12 months).
How much should he put aside each month?
Q3(e) Bags of crisps come in multi-packs of 4 bags per pack, costing 96p. How much is it per bag?

Q3(f) Julie is putting up shelves that are 1 metre long. How many will she get from a piece of wood 3.6 metres long?

## 4. Making sense of the answer - Rounding

Sometimes the answer you get can look a bit confusing at first. There might seem to be too many figures in the answer - or not enough.

## Example 4.1

You might need to round the answer to make sense of it. This can be particularly important when you are working out calculations using a calculator.

## 3 people share $£ 10$ between them. How much do they each get?

| They work out: $\quad £ 10 \div \mathbf{3}$ on a calculator and get the answer: |  |
| :--- | :--- |
| The answer will be in pounds. |  |
| So this shows: $\quad 3$ whole pounds <br> (before the decimal point) | and how many pence? <br> (after the decimal point) |


| Hint: The pence will be shown by the two numbers after the decimal point |
| :--- |
| Look at the number after these two (the 'decider') <br> to help you decide if you need to round up or round down <br>  <br> If the next number (the 'decider') is less than $5 \quad$ round down <br> If the next number (the 'decider') is 5 or more round up <br> In this example: The next number (the 'decider') is a 3. <br> So the amount is nearer to $£ 3.33$ <br> (round down) |

How much is each of these amounts when changed to money (pounds and pence)?
For each one, you will have to decide if you need to round up or down.

| Q 4 (a) $£ 12.379$ |  |
| :--- | :--- |
| Q | (b) $£ 1.999$ |
| Q | (c) $£ 5.942$ |
| $\mathbf{Q}$ | 4(d) $£ 4.251$ |
| Q | 4(e) $£ 10.8481$ |
| Q | (f) $£ 8.7175$ |
| Q | 4(g) $£ 9.6927$ |
| Q | (h) $£ 36.4563$ |

## Example 4.2

Four people need to pay a $£ 6$ taxi fare between them.
If you work out $£ 6 \div \mathbf{4}$ on a calculator, you get the answer:

## 1.5

How much is this in pounds and pence?
It is
$£ 1.50$
(but the calculator doesn't show the final 0)
Hint: If it was one pound five pence, this would show as 1.05.

Work out these calculations using a calculator and make sense of the answers you get:
4(i) Four friends win $£ 22$ between them.
If they share it equally, how much will they each get?
Q 4(j) Three people club together to buy a present for a friend.
The present costs $£ 16$. How much does each of them need to pay?
Q4(k) Luc is saving for spending money on his weekend away.
He wants to save up $£ 90$ over the next 4 weeks.
How much does he need to save per week?
Q 4(I) Packs of pizzas come in multi-packs of 3 pizzas per pack and cost $£ 2.40$.
How much is this per pizza?
Q 4(m) Lily gets $£ 25$ pocket money over 8 weeks. How much is this per week?

## 5. Checking your answer

You need to think about whether the answer you've got is reasonable and can be right. There is a range of ways that you can do this, including:

- Estimating answers
- Thinking about whether your answer is reasonable
- Using 'checking back' methods

If you would like practice with this, 'Mini-task: Which operation 2' looks at each of these in more detail.

## Using a problem-solving approach: Answer sheet

3. The units for the answers to the calculations are:

| Q3(a) | pounds | £18 $\div 3$ |
| :---: | :---: | :---: |
| Q 3(b) | drinks | How many $£ 1.99$ s can you get out of $£ 10$ ? |
| Q 3(c) | pounds | £30 $\div 5$ |
| Q 3(d) | pounds | £96 $\div 12$ |
| Q 3(e) | pence | $96 p \div 4$ |
| Q 3(f) | shelves | How many 1 metre lengths can you get out of 3.6 metres? |

4. The amounts in money are:

| Q 4(a) | $£ 12.38$ | (round up - because the next number was a 9) |
| :--- | :--- | :--- |
| Q 4(b) | $£ 2.00$ | (round up - because the next number was a 9) |
| Q 4(c) | $£ 5.94$ | (round down - because the next number was a 2) |
| Q 4(d) | $£ 4.25$ | (round down - because the next number was a 1) |

Hint for the next four answers: Don't be distracted by any numbers after the first three from the decimal point

| Q4(e) | $£ 10.85$ | (round up - the 'decider' was an 8) |
| :--- | :--- | :--- |
| $\mathbf{Q 4 ( f )}$ | $£ 8.72$ | (round up - the 'decider' was a 7) |
| $\mathbf{Q 4 ( g )}$ | $£ 9.69$ | (round down - the 'decider' was a 2) |
| $\mathbf{Q 4 ( h )}$ | $£ 36.46$ | (round up - the 'decider' was a 6) |

The calculations and answers are:

## Answer

| Q 4(i) | £5.50 |
| :---: | :---: |
| Q 4(j) | £5.33 |
| Q 4(k) | £22.50 |
| Q 4(I) | 80p |
| Q 4(m) | £3.13 |

## Calculation

$£ 22 \div 4=5.5$
$£ 16 \div 3=5.33333$
$£ 90 \div 4=22.5$
$£ 2.40 \div 3=0.8$
$£ 25 \div 8=3.125$

